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**BTECH**  
**(SEM III) THEORY EXAMINATION 2024-25**  
**MATHEMATICS-III**

TIME: 3 HRS

M.MARKS: 70

**Note:** 1. Attempt all Sections. If require any missing data; then choose suitably.

## SECTION A

1. Attempt all questions in brief.

2 x 7 = 14

a.	Write sufficient condition for $f(z)$ to be analytic.
b.	State Cauchy's integral theorem.
c.	Define Kurtosis.
d.	Write Binomial distribution.
e.	State Newton's divided difference formula.
f.	Describe Newton's one-third rule.
g.	Define Z-transform. or Define complex fourier transform.

## SECTION B

2. Attempt any three of the following:

7 x 3 = 21

a.	Show that the function $u = \frac{1}{2} \log(x^2 + y^2)$ is harmonic function.										
b.	Using method of Least squares, find the curve $y = a + b x^2$ that best fit the following data: <table border="1" style="margin: 5px auto;"> <tr> <td>x</td> <td>-1</td> <td>0</td> <td>1</td> <td>2</td> </tr> <tr> <td>y</td> <td>2</td> <td>5</td> <td>3</td> <td>0</td> </tr> </table>	x	-1	0	1	2	y	2	5	3	0
x	-1	0	1	2							
y	2	5	3	0							
c.	Using Euler's modified method solve $dy/dx = x+3y$ with the initial condition that $y=1$ when $x=0$ and hence find $y$ for $x = 1$ .										
d.	Use Runge-Kutta method of fourth order, solve $5 \frac{dy}{dx} = x^2 + y^2$ with $y(0) = 1$ , at $x = 0.2$ taking $h = 0.1$ .										
e.	Find the Fourier transform of $e^{-ax^2}$ , where $a > 0$ . or Find the Z-transform of $\cosh\left(\frac{k\pi}{2} + \alpha\right)$ .										

## SECTION C

3. Attempt any one part of the following:

7 x 1 = 7

a.	Evaluate the following integral using Cauchy integral formula $\int \frac{4-3z}{z(z-1)(z-2)} dz$ , where $C$ is the circle $ z  = 3/2$ .
b.	Expand $\frac{1}{z^2-3z+2}$ in the region $ z  < 1$ .

4. Attempt any one part of the following:

7 x 1 = 7

a.	If 10% of bolts produced by a machine are defective. Determine the probability that out of 10 bolts, chosen at random i) 1 ii) none iii) at most two bolts will be defective.
b.	If there are three misprints in a book of 1000 pages find the probability that a given page will contain i) no misprints ii) more than 2 misprints.



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5. **Attempt any one part of the following:** 7 x 1 = 7

a.	By using Newton-Raphson method, find the root of $x^3 - 2x + 0.5 = 0$ .				
b.	Using Lagrange's interpolation formula, find the values of y corresponding to x=3 from the following table:				
	x	0	1	2	4
	y	580	556	520	385

6. **Attempt any one part of the following:** 7 x 1 = 7

a.	Solve by Crout's method, the following system of equation : $3x + 2y + 7z = 4$ , $2x - 3y + z = 5$ , $3x + 4y + z = 7$ .
b.	Using Picard's method find a solution of $\frac{dy}{dx} = x + y^2$ ; $y(0) = 1$ .

7. **Attempt any one part of the following:** 7 x 1 = 7

a.	Find the Fourier sine transform of $\frac{e^{-ax}}{x}$ , $a > 0$ . Hence find Fourier sine transform of $\frac{1}{x}$ .
b.	Determine the largest Eigen value and the corresponding Eigen vector of the following matrix
	$\begin{bmatrix} 2 & -1 & 0 \\ -1 & 2 & -1 \\ 0 & -1 & 2 \end{bmatrix}$